



# UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

## **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/43

Paper 4 (Extended) May/June 2012

2 hours 15 minutes

Candidates answer on the Question Paper

Additional Materials: Geometrical Instruments

**Graphics Calculator** 

### **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, highlighters, glue or correction fluid.

You may use a pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. Answers in degrees should be given to one decimal place.

For  $\pi$ , use your calculator value.

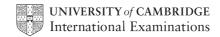
You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 120.

For Examiner's Use

This document consists of 20 printed pages.



## Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

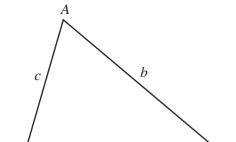
$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$



а

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area = 
$$\frac{1}{2}bc \sin A$$

			Answer all the questions.	
1	(a)		armer sows 600 tomato seeds. % of the seeds grow into plants.	
		Fine	d the number of seeds that grow into plants.	
			Answer(a) [2	2]
	(b)	(i)	The farmer sows 20 000 carrot seeds. 17 500 of these seeds grow into plants.	
			Calculate the percentage which did <b>not</b> grow into plants.	
			Answer(b)(i) % [2	2]
		(ii)	In one season the farmer sells 161.2 tonnes of carrots. This is 4% more than he expected to sell.	
			Calculate the number of tonnes he expected to sell.	
			Answer(b)(ii) tonnes [3	3]
	(c)	The	e farmer sows broccoli seeds, cabbage seeds and pumpkin seeds in the ratio	
			broccoli seeds : cabbage seeds : pumpkin seeds = 2 : 5 : 7 .	

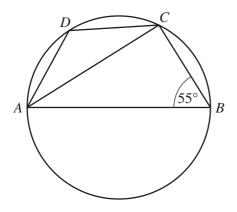
 $Answer(c) \qquad \qquad [2]$ 

The total number of seeds sown is 8400.

Find the number of cabbage seeds sown.

2 (a)

Examiner's Use



NOT TO SCALE

C and D are points on the circumference of a circle. AB is a diameter of the circle and angle  $ABC = 55^{\circ}$ .

Find

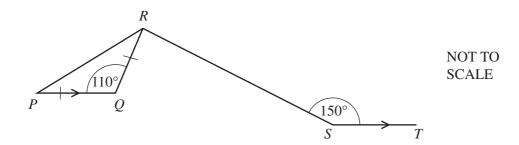
(i) angle ADC,

Answer(a)(i)	Γ1	1

(ii) angle CAB.

Answer(a)(ii)	 [1	]

**(b)** 



In the diagram angle  $PQR = 110^{\circ}$  and angle  $RST = 150^{\circ}$ . PQ = QR and PQ is parallel to ST.

Find

(i) angle PRQ,

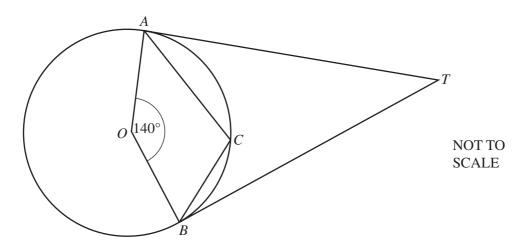
 $Answer(b)(i) \qquad [1]$ 

(ii) angle QRS.

*Answer(b)*(ii) [2]

(c)

For Examiner's Use



TA and TB are tangents to a circle centre O. C is a point on the circumference and angle  $AOB = 140^{\circ}$ .

(i) Find angle ATB.

Answer(c)(i)	[2]	ı
111111111111111111111111111111111111111	 12	

(ii) Find angle ACB.

(iii) On the diagram, draw the chord AB.

The radius of the circle is 5 cm. Calculate the length of the chord *AB*.

Answer(c)(iii) \_\_\_\_\_ cm [3]

3	In a scientific experiment the following six masses, in grams, were recorded.									
		$9.6 \times 10^{-5}$	$1.01 \times 10^{-4}$	$9.3 \times 10^{-5}$	1.04 ×	$10^{-4}$	$1.03 \times 10^{-4}$	9.8 ×	$10^{-5}$	
	(a)	Find the median	1.							
	(b)	Find the range.		Ans	wer(a)				g	[1]
	(c)	Calculate the m Give your answ	nean. Ever correct to 2 si						g	[1]
	(d)	Another mass, a The mean of the Find the value of	e seven masses i	ded.					g	[2]
				Ans	wer(d) x =	=			g	[3]

4	$f(x) = x^2 - 5$	g(x) = x - 2
7	$I(\Lambda)$ $\Lambda$ $J$	$S(x)$ $x \neq 2$

(a) Find the value of f(-2).

For Examiner's Use

**(b)** Solve f(x) = 4.

$$Answer(b) x = [2]$$

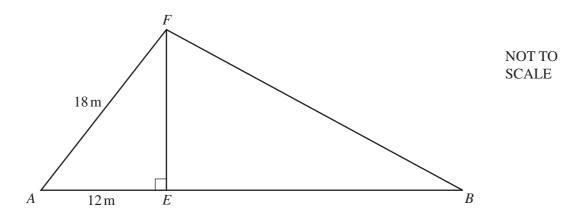
(c) Show that  $f(g(x)) = x^2 - 4x - 1$ .

**(d)** Solve f(g(x)) = f(x).

$$Answer(d) x =$$
 [2]

5

For Examiner's Use



EF is a vertical flagpole.

Two ropes, AF and BF, keep the flagpole in position.

The points A, E and B all lie in a straight line on horizontal ground.

 $AF = 18 \,\text{m}$  and  $AE = 12 \,\text{m}$ .

(a) (i) Calculate the height of the flagpole, EF.

Answer	(a)(	(i)	m	[2]	

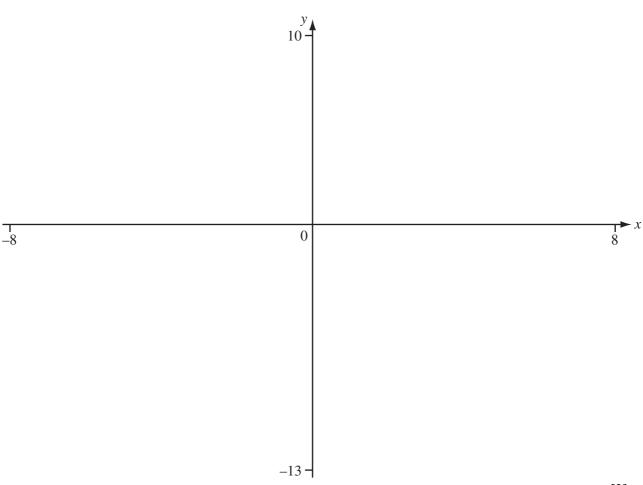
(ii) Calculate the size of angle *FAE*.

Answer(a)(ii) .....[2]

<b>(b)</b>	Angle $FAE = 2 \times \text{angle } FBE$ .							
	Show that $BE = 30.0 \text{m}$ , correct to 1 decimal place.	Examiner's Use						
	[3]							
(c)	Calculate the length of rope, BF.							
	Answer(c) m [2]							
(d)	P is on $BF$ so that $BP = 20$ m. Another rope, $EP$ , joins $E$ to $P$ .							
	Use the cosine rule to calculate the length of the rope, <i>EP</i> .							
	Answer(d) m [3]							

6 
$$f(x) = \frac{x^2 - 5x + 6}{x - 1}$$
, for  $-8 \le x \le 8$ .

(a) On the diagram, sketch the graph of y = f(x).



[3]

**(b)** Write down the equation of the vertical asymptote.

(c) Find the range of f(x) for the domain  $-8 \le x \le 8$ .

Answer(c) [2]

(d)	Solve	f(x)	) = 0.

(e) On the diagram, sketch the graph of y = 3x - 2.

[2]

(f) Write down the co-ordinates of the points where  $\frac{x^2 - 5x + 6}{x - 1} = 3x - 2$ . Give each answer correct to 3 decimal places.

Answer(f) ( \_\_\_\_\_\_ , \_\_\_\_\_)

( ...... , ...... ) [2]

7	(a)	Rajiv invests \$525 at $x\%$ per year <b>simple</b> interest.
		After 3 years he has \$588.

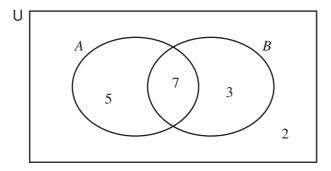
Find the value of x.

Answer(a) x =	[3]
Answer(a) x -	[3]

**(b)** A company's profits increase by 5% each year. In 2002 the profit was \$10 000.

Find the profit in 2010. Give your answer correct to the nearest \$100.

**8** (a) The Venn diagram shows the number of athletes (A) and the number of basketball players (B) in a class.



Use the Venn diagram to complete the following.

(i) 
$$n(A) =$$
 [1]

(ii) 
$$n(A \cap B') =$$
 [1]

(iii) 
$$n(A \cap B)' =$$
 [1]

(b) Each student in a school orchestra can play at least one of the piano, the violin and the trumpet.

For Examiner's Use

24 students play the piano

24 students play the violin

13 students play the trumpet

12 students play both the piano and the violin

7 students play both the piano and the trumpet

2 students play both the violin and the trumpet

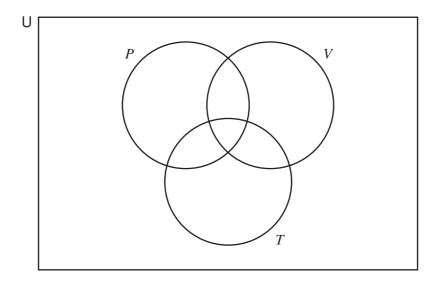
No student plays all three instruments

(i) Use this information to complete the Venn diagram below where

 $P = \{\text{students who play the piano}\},\$ 

 $V = \{\text{students who play the violin}\},\$ 

 $T = \{\text{students who play the trumpet}\}.$ 

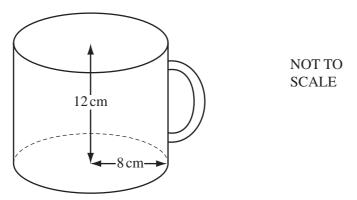


[3]

(ii) How many students are there in this orchestra?

*Answer(b)*(ii) ......[1]

9



For Examiner's Use

The diagram shows a large mug in the shape of a cylinder, open at the top. The internal radius of the mug is 8 cm and the internal height is 12 cm.

(a) Calculate the volume of water the mug holds when filled to the top.

Answer(a)	$cm^3$	[2]

**(b)** Calculate the **total** surface area of the inside of the mug.

(c)	500 cm <sup>3</sup> of water is poured into the mug.		
	Calculate the depth of water in the mug. Give your answer in centimetres correct to the nearest millimetre.		
			[2]
	Answer(c)	cm	[3]
(d)	The mug shown in the diagram is mathematically similar to a smaller mug. The volume of the smaller mug is $\frac{1}{8}$ of the volume of the larger one.		
	Find the radius of the smaller mug.		
	Answer(d)	cm	[2]

10 The lengths of 30 fish caught in a competition are recorded.

The length of each fish is measured correct to the nearest centimetre.

The results are shown in the ordered stem and leaf diagram.

Examiner's Use

1	1	1	2	4	5	6	7	8	9
2	0	4	5	7	9				
3	2	6	7	8	9				
4	3	4	6	7	8				
5	2	4	5						
6	3	4	9						

Key 3 | 2 means 32 cm

(a) Find the inter-quartile range.

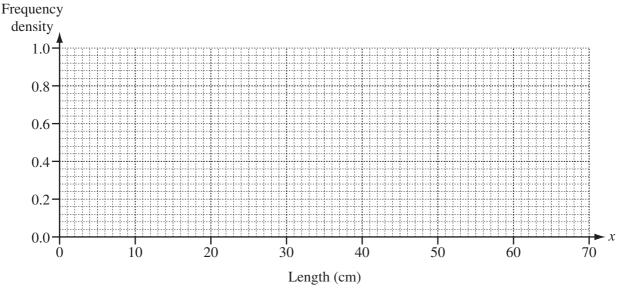
Answer(a) cm [2]

**(b)** Complete the table for the lengths of the 30 fish.

Class Interval	Frequency	Frequency density
$9.5 \le x < 14.5$		0.8
$14.5 \le x < 19.5$		
$19.5 \le x < 39.5$		
$39.5 \le x < 49.5$		
$49.5 \le x < 69.5$		

[4]

(c) On the grid, draw a histogram to show this information.

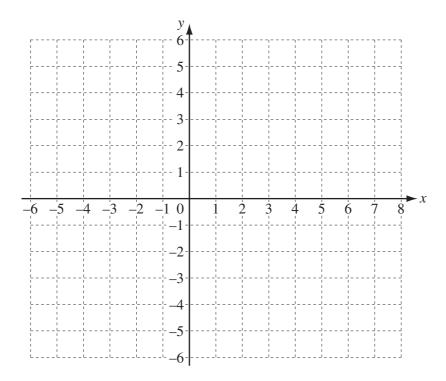


[3]

11	Gemma has these four cards.	
	I H L L	
	They are shuffled and placed face down on a table.	
	The cards are turned over, one at a time.	
	Find the probability that,	
	(a) the first card turned over is $H$ ,	
	Answer(a)	[1]
	Answer(b) $H$ ,	[2]
	Answer(c)	[3]
	(d) the cards are turned over in this order.	
	HILLL	
	Answer(d)	[2]

- 12 A quadrilateral has vertices P(0, 0), Q(4, 0), R(6, 4) and S(0, 2).
  - (a) On the grid, draw the quadrilateral *PQRS*.





[1]

- **(b)** On the same diagram,
  - (i) reflect PQRS in x = 0,

[1]

(ii) translate *PQRS* using the vector  $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$ ,

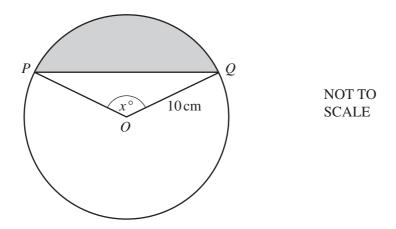
[2]

(iii) enlarge *PQRS*, centre (0, 0), scale factor  $\frac{1}{2}$ .

[3]

13

For Examiner's Use



The diagram shows a circle, centre O, radius 10 cm. PQ is a chord and angle  $POQ = x^{\circ}$ .

(a)	Write down,	in terms	of x and $\pi$	π, an expression	for the area	of the sector	POQ

<b>(b)</b>	Weite down in towns of v on expression		of the triengle POO	cm <sup>2</sup>	[2]
(D)	Write down, in terms of $x$ , an expression	ioi ille alea (	of the triangle FOQ.		
		Answer(b)		cm <sup>2</sup>	[2]
(c)	Write down, in terms of $x$ and $\pi$ , an expre	ession for the	area of the shaded segment.		
		Answer(c)		$cm^2$	[1]
(d)	The area of the <b>triangle</b> $POQ$ is 25 cm <sup>2</sup> . Angle $POQ$ is obtuse.				
	Show that $x = 150$ .				

[3]

(e) Find the area of the shaded segment.

Answer(e) \_\_\_\_\_ cm<sup>2</sup> [2]

Question 14 is on the next page.

14	4 A regular pentagon is drawn inside a circle so that its vertices lie on the circumference of the circle.  The length of each side of the pentagon is 4 cm.						
	(a)	Sketch a diagram to show this information.	Use				
		[1]					
	<b>(b)</b>	Calculate the radius of the circle.					
		Answer(b) cm [4]					

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.